

Chapter 03: Computer Arithmetic

Lesson 10

BCD Arithmetic Operations, Packed Decimals and Unpacked Decimals

Objective

- Understand the BCD
- BCD Numbers
- BCD Operations
- Packed Decimal
- Unpacked Decimal

BCD numbers

BCD Representation

- **Decimal 0** 0_{d0}
- **BCD Representation 0000 0000** $_{bcd}$

BCD Representation

- **Decimal 9** $0d9$
- **BCD Representation** $0000\ 1001_{bcd}$

BCD Representation

- **Decimal 10** $0d10$
- **BCD Representation** $0001\ 0000_{bcd}$

BCD Representation

- **Decimal 12** $0d12$
- **BCD Representation 0001 0010** $_{bcd}$

BCD Representation

- **Decimal 85** $0d85$
- **BCD Representation** $1000\ 0105_{bcd}$

The BCD representations of the decimal number 47 and binary number 0b01001000

- Decimal number 47 is denoted in BCD as $0d47 = 0100\ 0111_{bcd}$
- Binary number $0b01001000 = 2^6 + 2^3 = 64_d + 8_d = 0d72 = 0111\ 0010_{bcd}$

BCD operations

BCD arithmetic

- BCD arithmetic— using binary arithmetic
- The results adjusted to obtain the BCD number

Example: Adding BCD numbers 0d89 and 0d22

- The BCD numbers $0d89 = 1000\ 1001_{bcd}$ and $0d22 = 0010\ 0010_{bcd}$
- Step 1
- First perform binary addition of BCD numbers, as if they were binary numbers
- Generate an auxiliary carry (AC) if the addition $(x_3 + y_3)$ at b_3 location caused a carry

Step 1

- $1000 \mathbf{1}001_{\text{bcd}} + \underline{0010 \mathbf{0}010}_{\text{bcd}} = \underline{1010 \overset{\leftarrow}{1}011}$
- At bit 3, there is no carry, $AC = 0$

Step 2

- Perform the BCD adjust operation by adding 6 wherever required

Step 2 for adjusting the result of BCD addition in step 1

- $$\begin{array}{r}
 1000\ 1001_{bcd} \\
 + \underline{0010\ 0010}_{bcd} \\
 \hline
 1010\ 1011 \\
 \quad \underline{0110} \text{ Add 6 because lower digit } > 9 \\
 \hline
 1010\ 0001 \text{ AC generated 1} \\
 \underline{0001} \text{ so add 1 in the next digit} \\
 \hline
 101\hat{1}\ 0001
 \end{array}$$

Step 2

1011 0001

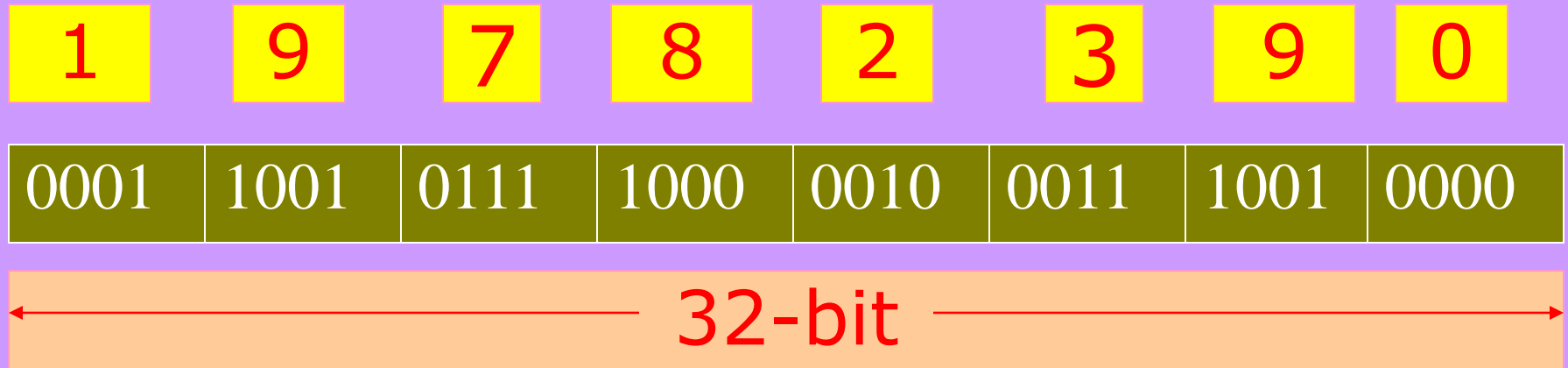
0110 Add 6 in upper digit as it is >0d9

1 0001 0001 Carry from bit 7 = 1

This number represents 100010001bcd
and is answer 0d111

Packed Decimal

Example: Packing 19782390 in 32-bit memory



Unpacked Decimal

Example: Unpacking 19782390 in 32-bit memory as unpacked decimals

1

9

7

8

00000001 00001001 00000111 00001000

2

3

9

0

00000010 00000011 00001001 0000 0000

← 64-bit →

Summary

We learnt

- BCD Representation
- BCD Operations using AC
- Packed Decimal
- Unpacked Decimals

End of Lesson 10 on
**BCD Arithmetic Operations, Packed
Decimals and Unpacked Decimals**